David Rojas Universitat Autònoma de Barcelona, Spain

MONOTONOUS PERIOD FUNCTION FOR EQUIVARIANT DIFFERENTIAL EQUATIONS WITH HOMOGENEOUS NONLINEARITIES

Real planar autonomous analytic differential systems can be written in complex coordinates in the compact form $\dot{z} = F(z, \overline{z}), z \in \mathbb{C}$. The \mathbb{Z}_k -equivariant differential equations are equations of this form that are invariant under a rotation through the angle $2\pi/k$ about the origin. For them, the phase portrait on each sector of width $2\pi/k$ centered at the origin is repeated k times. In this paper we are concerned with the simplest family of polynomial \mathbb{Z}_k -equivariant differential equations with a non-degenerated center at the origin and homogeneous nonlinearities

$$\dot{z} = iz + a(z\overline{z})^n z^{k+1},\tag{1}$$

with n and k a positive integers and $0 \neq a \in \mathbb{C}$. The qualitative properties of the period function associated to the origin was posed as the 16th open problem in [A. Gasull. Some open problems in low dimensional dynamical systems. SeMA Journal 78 (2021) 233–269]. In particular, it is conjectured that it is monotonous decreasing. In this talk we give a positive answer to such conjecture. We show this result as corollary of proving that the period function of the center at the origin of a sub-family of the reversible quadratic centers is monotonous decreasing as well. The results presented in this talk can be found in [A. Gasull and D. Rojas. Monotonous period function for equivariant differential equations with homogeneous nonlinearities. Mediterr. J. Math. 22 (2025) 112].