Global dynamics of the Kummer–Schwarz differential equation

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In this talk/poster we present the study of the Kummer–Schwarz differential equation $2\dot{x}\dddot{x} - 3\ddot{x}^2 = 0$ which is of special interest due to its relationship with the Schwarzian derivative. This differential equation is transformed into a first order differential system in $\mathbb{R}^3$, and we provide a complete description of its global dynamics adding the infinity.

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