Distributional chaos for the solutions of certain partial differential equations

Xavier Barrachina¹, J.Alberto Conejero²

¹ Institut Universitari de Matemàtica Pura i Aplicada, 46022 València, Spain. *E-mail address:* xabarci@doctor.upv.es

² Institut Universitari de Matemàtica Pura i Aplicada, 46022 València, Spain. E-mail address: aconejero@upv.es URL: http://albertoconejero.webs.upv.es

In the study of the dynamics of linear operators defined on Banach spaces, interesting phenomena appear when we consider an underlying infinite-dimensional setting. Several notions of chaos, such as the ones of Devaney and Auslander & Yorke (hypercyclicity), have been already considered for linear operators and C_0 semigroups of operators that give the solution of certain abstract Cauchy problems. We refer to the monograph by Grosse-Erdmann and Peris [2] for further information on these topics.

The notion of distributional chaos has been recently added to the study of the chaoticity of linear operators [3]. We will report some results concerning how does it works on C_0 -semigroups of operators. In particular several examples of partial differential equations that present this behaviour will be provided. More-over, we will provide an example of a C_0 -semigroup with a full scrambled set.

References

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