

# IMUB October 2017

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Caltech

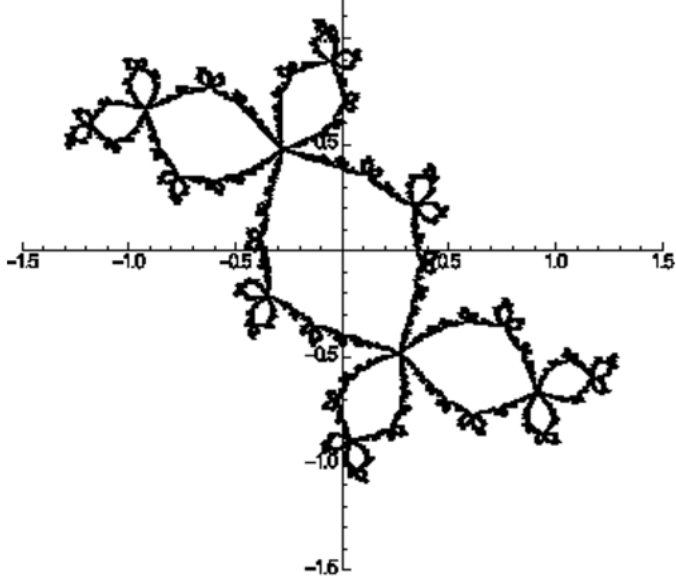
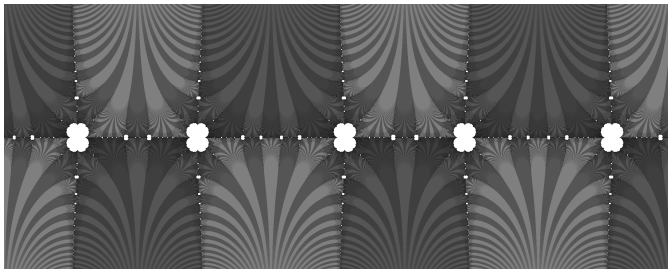


Figure: <https://www.math.vt.edu/netmaps/followrabbit.php>,  
 $c \approx -0.122561 + 0.744862i$



**Figure:** the dynamical plane of  $z + \sin(z) + 2\pi$  (source for picture: Lasse Rempe-Gillen)

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Theorem (Bishop 2014): wandering domains **do** occur in  $\mathcal{B}$ .

Theorem (Baker 1976): wandering domains exist for some entire functions.

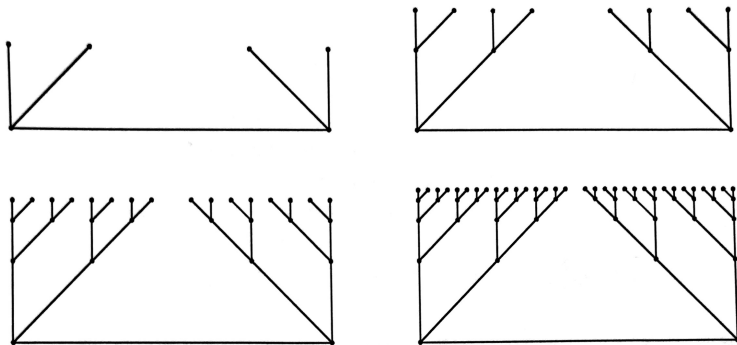


Figure 8. The basic building blocks are pairs of binary trees. Shown are the trees  $\hat{T}_1$ ,  $\hat{T}_2$ ,  $\hat{T}_3$  and  $\hat{T}_4$ .



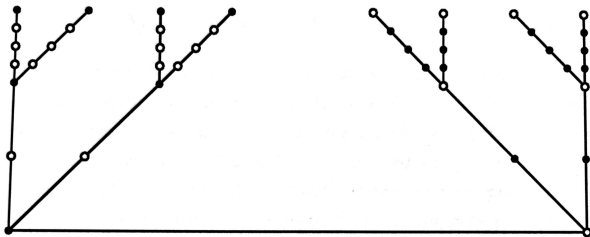
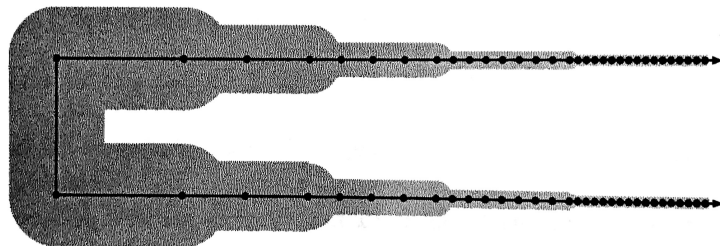
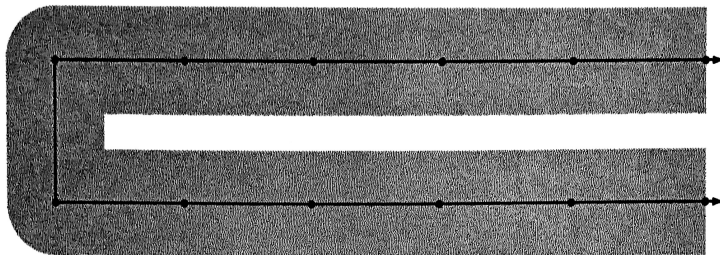


Figure 9. We add vertices to  $\widehat{T}_j$  to get  $T_j$ . The  $j$ th level is divided into  $2^j$  equal subedges by adding extra vertices. We illustrate only the  $j=2$  case, since it's hard to see individual vertices at higher levels; most of our figures will not show these vertices at all, but their presence is essential to the construction.



# References



Chris Bishop (2014)

Constructing Entire Functions By Quasiconformal Folding

*Acta Mathematica*



Nuria Fagella, Sebastien Godillion, and Xavier Jarque (2014)

Wandering domains for composition of entire functions

*Journal of Mathematical Analysis and Applications*