ON CONSTRUCTING ENTIRE FUNCTIONS BY QUASICONFORMAL FOLDING

KIRILL LAZEBNIK, STONY BROOK UNIVERSITY

The problem of deciding which classes of entire functions can have wandering domains has roots in Sullivan's no wandering domain theorem [Sul85] for rational maps. Shortly afterwards the proof was adopted to show that transcendental maps with finitely many singular values can not have wandering domains [GK86], [EL87]. It was already known that for general transcendental entire maps with unbounded singular set, wandering domains can exist. The Eremenko-Lyubich class $\mathcal{B}$ consists of those transcendental maps whose singular set is bounded. In [Bis14], Bishop constructs an entire function in $\mathcal{B}$ with wandering domain. We exposit first the main theorem in [Bis14] which is a more general method for constructing entire functions with prescribed critical and singular values. Then we explain how this theorem is applied to construct functions in $\mathcal{B}$ with wandering domain.

REFERENCES

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