JULIA SETS OF POSITIVE MEASURE

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ABSTRACT. This will be an overview of the proof of the existence of Julia sets with positive measure.

Provisional plan

Course 1: Semi-continuity of Julia set and Lebesgue measure, and Douady's approach. Perturbations of Siegel disks and parabolic points, computer experiments. Douady's conjectures implying existence of positive measure Julia sets.

Course 2: Jellouli's computation, parabolic explosion, proof of one of Douady's conjectures. Second conjecture : computer experiments and reformulation. Reduction.

Course 3: The renormalization of Inou and Shishikura. Consequences: bound on the height of cylinders and semi-continuity of the post-critical set. Mc Mullen's theorems. Proof of the second conjecture.