

A dynamic Parrondo's paradox for continuous seasonal systems*

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Abstract

We show that planar continuous alternating systems, which can be used to model systems with seasonality, can exhibit a type of Parrondo's dynamic paradox, in which the stability of an equilibrium, common to all seasons is reversed for the global seasonal system.

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